

# Least Square Fit

**Spoken Tutorial Project**

**<http://spoken-tutorial.org>**

**National Mission on Education through ICT**

**<http://sakshat.ac.in>**

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**2 April 2018**



# Learning Objectives



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- ▶ **Generate the least square fit line for a given set of points**



# System Specifications



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## ▶ Ubuntu Linux 16.04



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- ▶ **Ubuntu Linux 16.04**
- ▶ **Python 3.4.3**



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- ▶ **Ubuntu Linux 16.04**
- ▶ **Python 3.4.3**
- ▶ **IPython 5.1.0**



# Pre-requisite



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## ▶ Using plot interactively



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- ▶ Loading data from files



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- ▶ **Using arrays and matrices**



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- ▶ **Theoretical knowledge of least square method**



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# Pre-requisite

- ▶ Using plot interactively
- ▶ Loading data from files
- ▶ Using arrays and matrices
- ▶ Theoretical knowledge of least square method

If not, see the relevant Python tutorials on <http://spoken-tutorial.org>



# Pendulum.txt



# Pendulum.txt

- ▶ Please download the file `pendulum.txt` from the Code files link of this tutorial



# Pendulum.txt

- ▶ Please download the file **pendulum.txt** from the **Code files** link of this tutorial
- ▶ **Save it in the current working directory**



# Example

- ▶ **Generate a least square fit line for  $L v/s t^2$  using the data in the file pendulum.txt**



# Least Square Fit line

- ▶ Fit a line through points for the equation  $T^2 = m * L + c$



# Least Square Fit line

- ▶ Fit a line through points for the equation  $T^2 = m * L + c$
- ▶ where **m** represents the slope of the line and **c** represents the intercept of the line



# Least Square Fit line

- ▶ Fit a line through points for the equation  $T^2 = m * L + c$
- ▶ where **m** represents the slope of the line and **c** represents the intercept of the line
- ▶ We will obtain **m** and **c** using linear regression



# Steps for Least Square Fit line



# Steps for Least Square Fit line

- ▶ First generate the two matrices  $tsq$  and  $A$



# Steps for Least Square Fit line

- ▶ First generate the two matrices `tsq` and `A`
- ▶ Use the `lstsq` function to find the values of the slope `m` and intercept `c`



# Matrix Formulation

- ▶ In matrix form, the equation can be represented as  $tsq = A * p$



# Matrix Formulation

- ▶ In matrix form, the equation can be represented as  $tsq = A * p$
- ▶  $tsq$  is a one-dimensional array of size  $n$



# Matrix Formulation

$$\text{tsq} = A * p$$

▶ **A** is a matrix of size  **$n \times 2$**



# Matrix Formulation

$$\text{tsq} = \mathbf{A} * \mathbf{p}$$

- ▶  $\mathbf{A}$  is a matrix of size  $n \times 2$ 
  - ▶ The first column will contain the length of the pendulum



# Matrix Formulation

$$\text{tsq} = A * p$$

- ▶ **A** is a matrix of size  **$n \times 2$** 
  - ▶ The first column will contain the length of the pendulum
  - ▶ **The second column will contain the number 1**



# Matrix Formulation

$$\text{tsq} = \mathbf{A} * \mathbf{p}$$

- ▶  $\mathbf{p}$  is a one-dimensional array of size 2



# Matrix Formulation

$$\text{tsq} = \mathbf{A} * \mathbf{p}$$

- ▶  $\mathbf{p}$  is a one-dimensional array of size 2
  - ▶ The first row contains the slope of the line



# Matrix Formulation

$$tsq = A * p$$

- ▶ **p** is a one-dimensional array of size 2
  - ▶ The first row contains the slope of the line
  - ▶ The second row contains the intercept of the line



# Matrix Formulation

**p** is  $\begin{bmatrix} m \\ c \end{bmatrix}$

We need to find  $p$  to plot the line



# Summary

- ▶ **Generate a least square fit using matrices**
- ▶ **Use the function `lstsq()` to generate a least square fit line**



# Evaluation

## 1. What does `ones_like([1, 2, 3])` produce

- ▶ `array([1, 1, 1])`
- ▶ `[1, 1, 1]`
- ▶ `[1.0, 1.0, 1.0]`
- ▶ **Error**



# Solution

```
1. array([1, 1, 1])
```



# Forum to answer questions

- ▶ Do you have questions in **THIS Spoken Tutorial?**
- ▶ Choose the minute and second where you have the question.
- ▶ Explain your question briefly.
- ▶ Someone from the **FOSSEE** team will answer them. Please visit

<http://forums.spoken-tutorial.org/>



# Forum to answer questions

- ▶ Questions not related to the Spoken Tutorial?
- ▶ Do you have general / technical questions on the Software?
- ▶ Please visit the FOSSEE Forum  
<http://forums.fossee.in/>
- ▶ Choose the Software and post your question.



# Textbook Companion Project

- ▶ **The FOSSEE team coordinates coding of solved examples of popular books**
- ▶ **We give honorarium and certificate to those who do this**

**For more details, please visit this site:**

<http://tbc-python.fossee.in/>



# Acknowledgements

- ▶ **Spoken Tutorial Project is a part of the Talk to a Teacher project**
- ▶ **It is supported by the National Mission on Education through ICT, MHRD, Government of India**
- ▶ **More information on this mission is available at:**

<http://spoken-tutorial.org/NMEICT-Intro>



# THANK YOU!

For more information, visit our website  
<http://fossee.in/>

